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# Dynamic Model of Hip and Ankle Joints Loading during Working with a Motorized Backpack Sprayer

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#### Abstract

The main objective of this paper is to develop a seven-link dynamic model of the operator's body while working with a motorized backpack sprayer. This model includes the coordinates of the sprayer relative to the body, the rotational inertia of the sprayer, the muscle moments acting on the joints, and a kinematic coupling that keeps the body balanced between the two legs. The constraint functions were determined and the non-linear differential equations of motion were derived using Lagrangian equations. The results show that undesirable fluctuations in the ankle force are noticeable at the beginning and end of a swing phase. Therefore, injuries to the ankle joint are more likely due to vibrations. The effects of engine speed and sprayer mass on the hip and ankle joint forces were then investigated. It is found that the engine speed and sprayer mass have significant effects on the hip and ankle forces and can be used as effective control parameters. The results of the analysis also show that increasing the engine speed increases the frequency of the hip joint force. However, no significant effects on the frequency of the ankle joint force are observed. The results of this study may provide researchers with insight into estimating the allowable working hours with the motorized backpack sprayers, prosthesis design, and load calculations of hip implants in the future.

Keywords: Lagrange equation, Operator, Vibration, Weight of sprayer

#### Symbols and Abbreviations

Parameter	Description	Unite
$c_b$	Distance from hip joint to center of mass (CoM) of upper body	m
$c_f$	Distance from the ankle joint to CoM of the foot	m
$C_s$	Distance from the knee joint to the CoM of the shank	m
$C_t$	Distance from hip joint to CoM of the thigh	m
е	Unbalance mass eccentricity	mm
g	Gravitational acceleration	ms <sup>-2</sup>
$I_{sp}$	Mass moments of inertia of sprayer about its principal axis	kg.m <sup>2</sup>
ĺ	Stance leg length	m



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$l_s$	Shank length	m
$l_t$	Thigh length	m
$m_o$	Unbalance mass of sprayer engine	gr
$m_b$	Upper body mass	kg
$m_f$	Foot mass	kg
$m_h$	Hip mass	kg
$m_l$	Leg mass	kg
$m_s$	Shank mass	kg
$m_{sp}$	Sprayer mass	kg
$m_t$	Thigh mass	kg
$(x_{sp}, y_{sp})$	Sprayer position from the CoM of the upper body	(m, m)
ω	Engine speed	rpm
$x_h$	Horizontal coordinate of hip joint	M
$v_h$	Vertical coordinate of the hip joint	М
$\theta_{I}$	The angle between the vertical axis and the stance leg	Radian
$\theta_2$	The swing angle between the vertical axis and the thigh	Radian
$\tilde{\theta_3}$	The angle between the vertical axis and the upper body	Radian
$\theta_{2s}$	The swing angle between the vertical axis and the shank	Radian
$\theta_{2f}$	The angle between the horizontal axis and the foot	Radian

# Introduction

One of the most popular ways of crop protection against weeds and pests is applying motorized backpack sprayers. The use of the motorized backpack sprayer eliminates the need for hand pumping and is suitable for small-scale farms. However, the major disadvantage of motorized backpack sprayers is the external forces acting on the operator's body (Kouchakzadeh, & Beigzadeh, 2015).

Forces acting on the human body are important factors in the initiation and progression of joint disease (Astephen, Deluzio, Caldwell, & Dunbar, 2008). Force analysis of hip and ankle joints can be useful in the development of strategies to avoid and manage conditions such as osteoarthritis and deterioration of femoroacetabular (Correa, Crossley, Kim, & Pandy, 2010). Force analysis of hip and ankle joints requires multi-segment models.

Several researches have been done on the dynamic modeling of the human body. Kuo (2001) applied a simple model of bipedal walking to evaluate simple hypotheses for the metabolic cost of muscle activity. Tlalolini, Chevallereau, & Aoustin (2010) optimized the walking motions of a bipedal model by minimizing the value of the torque. The optimization process was carried out with and without the rotation of the supporting foot about the toe. Huang, Wang, Chen, Xie, & Wang (2012) employed a seven-link dynamic bipedal walking model with flat feet to analyze the dynamics of walking. The results indicated that ankle stiffness plays different roles in different gaits. Martin & Schmiedeler (2014) proposed four and six link planar biped models with knees and rigid circular feet; The ankle was not considered in the four link model. The results showed that the model with ankles is more accurate in predicting energy consumption during normal human walking at different speeds. Sharbafi & Seyfarth (2015) utilized a five link model with a rigid upper body and two segmented legs to extract internal relations between the joints' angles and stance leg orientation which hold the configuration harmonized during the gaits. Jena, Kumar, Singh, & Mani (2016) developed a biomechanical model to predict metabolic energy consumption for carrying load manually by varying modes (head, shoulder, and back), loads, and ground inclinations. The results indicated that frontal torque (in shoulder mode) requires higher physiological energy than sagittal torque. Ma, Xu, Fang, Lv, & Zhang (2022) present the dynamic model of the human-prosthesis heterogeneous coupled system. Ma, Xu, & Zhang (2023) also applied control strategies for prosthesis walking on stochastically uneven terrain.

Mechanical actions of muscles are necessary for dynamical modeling of the human body and can be considered as moments applied at the joints. Weiss, Kearney,

& Hunter (1986) indicated that the momentangle relationships in the hip, knee, and ankle joints are similar to that of a non-linear spring. Maletsky & Hillberry (2005) designed a dynamic knee simulator to reproduce the loading and kinematics of the human knee during different activities. Lim & Park (2018) developed a model for human locomotion with a curvy foot connected to a leg by a springy segment. Thus, the oscillations of the center of mass during walking can be described by the mechanics of a simple passive Spring Loaded Inverted Pendulum (SLIP). Kim, Lee, & Koo (2018) simulated joint reaction forces, active moments by muscles, and passive moments by connective tissues. They found that, at Chopart and Lisfranc joints, passive moments were responsible for large portions of the net moment. The passive structures and passive moments in the midfoot joints provide strength and prevent injuries.

Carrying backpack loads for long distances is common in a range of human activities. As a result, the influence of backpack carriage on physical performance has been investigated to establish guidelines for safe load limits. Liu (2007) analyzed the effect of backpack load position, walking speed, and surface grade on physiological responses of infantry the soldiers. The results confirmed that positioning the backpack mass center as near as possible to the body mass center resulted in the lowest energy consumption. Alamoudi, Travascio, Onar-Thomas, Eltoukhy, & Asfour (2018) determined the effect of different carrying methods on walking stability using motion capture analysis. The results confirmed that the lack of stability in the frontal carriage forced the body to increase the cadence to maintain stability. Additionally, to minimize the moment generated by both the upper body and the heavy load, participants tended to decrease the length of their stride. Walsh, Low, & Arkesteijn (2018) studied the effect of stable and unstable load carriage on walking gait variability, dynamic stability, and muscle activity of older adults. The results showed that unstable load carriage reduces dynamic stability compared to unloaded walking.

Reviewing the literature reveals that the investigation of the joint forces during load carrying is important for preventing joint injuries. However, to date, no research has been published on the joint forces during the working with the motorized backpack sprayers. Therefore, the initial objective of the present study is to develop a seven-link dynamic model of the operator's body while working with a motorized backpack sprayer. The secondary goal of this research is to examine the effects of different working conditions (engine speed and mass of sprayer) on the hip and ankle joint forces. This is a continuation of our previous work, where the torque-angle relationships in the hip, knee, and ankle joints for the backpack sprayer operator body were discussed (Karimi Avargani, Maleki, Besharati, & Ebrahimi, 2020).

# **Materials and Methods**

In this section, the principle of the Lagrange equation for nonholonomic constraints is introduced. The total kinetic energy, potential energy, generalized forces, and constraints are expressed for the proposed model. The nonlinear equations of motion are formulated using Lagrangian equations and solved using Maple software (Ver 2015).

# Lagrange Equation for Nonholonomic Constraints

Lagrangian equations have a special place in analytical mechanics. They represent equations of motion in terms of generalized coordinates. A holonomic constraint in the system of n generalized coordinates  $q_i$  can be written as Eq. 1.

$$g_i(q_1, q_2, ..., q_n, t) = 0$$
 (1)

For nonholonomic constraints, Eq. 1 changes into a differential form in Eq. 2 (D'Souza & Garg, 1984; Greenwood, 1988):

$$\sum_{\nu=1}^{n} a_{l\nu} dq_{\nu} + a_{lt} dt = 0 \quad l=1, 2, \dots, s$$
 (2)

Where v=1, 2, ..., n and l=1, 2, ..., s are the number of coordinates and number of constraints, respectively (n>s). Eq. 3 expresses

Lagrange's equation for constrained systems.  $d = \frac{\partial T}{\partial t} = \frac{\partial V}{\partial t} = \frac{\delta V}{\delta t}$ 

$$\frac{u}{dt}\left(\frac{\partial I}{\partial \dot{q}_{\nu}}\right) - \frac{\partial I}{\partial q_{\nu}} + \frac{\partial v}{\partial q_{\nu}} - \sum_{l=1} \lambda_{l} a_{l\nu} = Q_{\nu} \quad \nu = 1, 2, \dots, n \quad (3)$$

Where T, V,  $\lambda_l$ , and  $Q_v$  are kinetic energy, potential energy, Lagrange's coefficients, and generalized force related to generalized coordinate  $q_i$ , respectively. These *n* equations have n+s unknowns, namely the *n* coordinates  $(q_v)$  and the *s* Lagrange multipliers  $(\lambda_l)$ . The additional equations (Eq. 2) are needed for the s constraint which is coupled with the  $q_v$ . However, as shown in Eq. 4, these are considered as differential equations.

$$\sum_{\nu=1}^{n} a_{l\nu} \dot{q}_{\nu} + a_{lt} = 0 \quad l = 1, 2, \dots, s$$
(4)

Dynamic model of operator's body during spraying

Fig. 1 shows the proposed dynamical model of the operator's body during working with a motorized backpack sprayer. This model includes two rigid legs connected to the rigid upper body with hinges at the hips. Each leg includes the thigh, shank, and foot. The thigh and the shank are connected at the knee joint and the foot and the shank are connected at the ankle joint. A point mass  $m_h$  at the hip represents the pelvis. The mass of upper body  $m_b$ , leg  $m_l$ , thigh  $m_t$ , shank  $m_s$ , and foot  $m_f$  are considered lumped parameters. Longitudinal parameters  $c_b$ ,  $c_f$ ,  $c_l$ ,  $c_s$ ,  $c_t$ , l,  $l_s$ , and  $l_t$  are distances from the hip joint to the Center of Mass (CoM) of upper body, from the ankle joint to CoM of foot, from the hip joint to CoM of stance leg, from knee joint to CoM of shank, from the hip joint to CoM of thigh, stance leg length, shank length, and thigh length, respectively. The motorized backpack sprayer is located at position  $(x_{sp}, y_{sp})$  from the CoM of the upper body.



Fig.1. The proposed dynamical model of the operator's body while working with a motorized backpack sprayer

The total kinetic energy, potential energy, generalized forces, and constraints are expressed using the following assumptions (Wisse, Schwab, & van der Helm, 2004):

- The joints have no damping or friction.
- Bones do not suffer from flexible deformation.
- A kinematic coupling has been used in the model to keep the body midway between the two legs.

- The shank of the foot stance is always locked and the whole leg can be modeled as one rigid stick.
- There is enough friction between the walker and the ground. Thus, a flat foot does not deform or slip.
- The muscle moments acting on the hip, knee, and ankle joints are modeled as non-linear torsional springs.
- The sprayer engine is an unbalanced force. This can be caused by the deposition or erosion of the rotational parts.

# **Kinetic Energy**

As shown in Fig. 1, it is assumed that the *x*-axis is along the ground while the *y*-axis is vertical to the ground pointing upward. The dynamic model for the operator's body while working with a motorized backpack sprayer can be described by the generalized coordinates (Eq. 5).

$$q^{T} = [x_{h}, y_{h}, \theta_{1}, \theta_{2}, \theta_{3}, \theta_{2s}, \theta_{2f}]$$
(5)

Where  $x_h$ ,  $y_h$ ,  $\theta_1$ ,  $\theta_2$ ,  $\theta_3$ ,  $\theta_{2s}$ , and  $\theta_{2f}$  are the horizontal coordinate of hip joint, vertical coordinate of hip joint, the angle between vertical axis and the stance leg, the swing angle between vertical axis and the thigh, the angle between vertical axis and the upper body, the swing angle between vertical axis, and the shank and the angle between horizontal axis and foot, respectively. The positive direction of all the angles is counterclockwise. The total kinetic energy of the system is defined as the sum of the kinetic energy of the point masses, and the translational and rotational kinetic energy of backpack the motorized sprayer. The expression for the kinetic energy is obtained in Eq. 6.

$$T = T_{h} + T_{i} + T_{i} + T_{h} + T_{sp} + T_{s} + T_{f}$$

$$= \frac{1}{2} [m_{h} + m_{l} + m_{i} + m_{h} + m_{sp} + m_{s} + m_{f}]\dot{x}_{h}^{2}$$

$$+ \frac{1}{2} [m_{h} + m_{l} + m_{i} + m_{h} + m_{sp} + m_{s} + m_{f}]\dot{y}_{h}^{2}$$

$$+ \frac{1}{2} [m_{i}c_{i}^{2}\dot{\theta}_{i}^{2} + \frac{1}{2} [m_{i}c_{i}^{2} + m_{s}l_{i}^{2} + m_{f}l_{i}^{2}]\dot{\theta}_{2}^{2}$$

$$+ \frac{1}{2} [I_{sp} + m_{b}c_{b}^{2} + m_{sp} [(c_{b} + y_{sp})^{2} + x_{sp}^{2}]]\dot{\theta}_{3}^{2}$$

$$+ \frac{1}{2} [m_{s}c_{s}^{2} + m_{f}l_{s}^{2}]\dot{\theta}_{2s}^{2} + \frac{1}{2} m_{f}c_{f}^{2}\dot{\theta}_{2f}^{2} + m_{i}c_{i}\dot{\theta}_{i}(\dot{x}_{h}\cos\theta_{i} + \dot{y}_{h}\sin\theta_{i})$$

$$- m_{c}c_{i}\dot{\theta}_{2}(\dot{x}_{h}\cos\theta_{2} - \dot{y}_{h}\sin\theta_{2}) + m_{b}c_{b}\dot{\theta}_{3}(\dot{x}_{h}\cos\theta_{3} - \dot{y}_{h}\sin\theta_{3})$$

$$+ m_{sp}\dot{\theta}_{3} \left\{ [(c_{b} + y_{sp})\dot{x}_{h} + x_{sp}\dot{y}_{h}]\cos\theta_{3} + [x_{sp}\dot{x}_{h} - (c_{b} + y_{sp})\dot{y}_{h}]\sin\theta_{3} \right\}$$

$$+ m_{i} \left\{ l_{c}\dot{\theta}\dot{\theta}_{2s}\cos(\theta_{2} - \theta_{2s}) - \dot{x}_{h} [l\dot{\theta}_{2}\cos\theta_{2} + c_{i}\dot{\theta}_{2s}\cos\theta_{2s}] + \dot{y}_{h} [l\dot{\theta}_{2}\sin\theta_{2} + c_{s}\dot{\theta}_{2s}\sin\theta_{2s}] \right\}$$

$$+ m_{f} \left\{ l_{i}\dot{\theta}\dot{\theta}_{2s}\cos(\theta_{2} - \theta_{2s}) - c_{i}l_{i}\dot{\theta}\dot{\theta}_{2f}\sin(\theta_{2f} - \theta_{2}) + c_{f}l_{i}\dot{\theta}\dot{\theta}_{2}\dot{\theta}_{2f}\sin(\theta_{2f} - \theta_{2s}) - c_{k} \left[ l\dot{\theta}_{2}\cos\theta_{2} + c_{i}\dot{\theta}_{2}\cos\theta_{2s} \right] \right\}$$

Where  $I_{sp}$  is the mass moment of inertia of the sprayer about its principal axis.

# **Potential Energy**

The total potential energy of the system is given in Eq. 7 and is defined as the sum of the gravitational energy of the point masses.  $U = U_{h} + U_{l} + U_{h} + U_{m} + U_{r} + U_{\ell}$ 

$$= -\left[m_{h}l + m_{l}(l - c_{l}) + m_{l}l + m_{b}l + m_{sp}l + m_{s}l\right]g(1 - \cos\theta_{1}) + \left[m_{r}c_{r} + m_{s}l_{r}\right]g(1 - \cos\theta_{2}) - \left[m_{b}c_{b} + m_{sp}(c_{b} + y_{sp})\right]g(1 - \cos\theta_{3}) + m_{y}gx_{sp}\sin\theta_{3} + m_{s}gc_{s}(1 - \cos\theta_{2s}) + m_{f}g(l\cos\theta_{1} - l_{r}\cos\theta_{2} - l_{s}\cos\theta_{2s} - c_{f}\sin\theta_{2f})\right]$$
(7)

#### **Generalized Forces**

The generalized forces acting on the operator's body while working with a motorized backpack sprayer include forces resulting from gravity and are unbalanced due to erosion of the sprayer engine, muscle moment acting on the hip joint, muscle moment acting on the knee joint, and muscle moment acting on the ankle joint. The generalized forces  $Q_{qi}$  are given by the following equations (Eq. 8-14).

$$Q_{\rm r} = m_0 e \omega^2 \cos(\omega t) \tag{8}$$

$$Q_{y_h} = m_0 e \omega^2 \sin(\omega t) \tag{9}$$

$$Q_{\theta_{\rm l}} = T_{1f} \tag{10}$$

$$Q_{\theta_2} = T_2 \tag{11}$$

$$Q_{\theta_3} = m_0 e \omega^2 \cos \omega t [(c_b + y_{sp}) \cos \theta_3 + x_{sp} \sin \theta_3]$$
(12)

 $+ m_0 e\omega^2 \sin \omega t [-(c_b + y_{sp})\sin \theta_3 + x_{sp}\cos \theta_3]$ (12)

 $Q_{\theta_{2s}} = T_{2s} \tag{13}$ 

 $Q_{\theta_{2\ell}} = 0$ 

Where  $m_0$ , e, and  $\omega$  are the unbalanced mass of the sprayer engine, the unbalanced mass eccentricity, and the engine speed, respectively.

The muscle moment acting on the hip joint  $T_2$  (the swing leg, Eq. 15), muscle moment acting on the knee joint  $T_{2s}$  (the swing leg, Eq. 16), and muscle moment acting on the ankle joint  $T_{1f}$  (stance leg, Eq. 17) are non-linear functions of the angle between the two segments (Karimi *et al.*, 2020).

$$T_2 = 0.0007(\theta_2 - \theta_3)^3 - 0.0258(\theta_2 - \theta_3)^2 + 0.3236(\theta_2 - \theta_3) - 1.6792$$
 (15)

$$T_{2s} = -0.0011(\theta_{2s} - \theta_2)^2 - 0.0029(\theta_{2s} - \theta_2) + 1.2683$$
(16)

$$T_{1f} = 0.0043\theta_1^3 + 0.0429\theta_1^2 + 0.5052\theta_1 + 3.1455$$
(17)

#### **Constraints**

A constraint can be expressed by a relationship between generalized coordinates and time. When foot contact with the ground is maintained, first and second constraint equations can be represented as Eq. 18 and 19.  $y_h - l\cos\theta_1 = 0$  (18)

$$x_h + l\sin\theta_1 - x_{ankle} = 0 \tag{19}$$

Here, the  $x_{ankle}$  is the fixed position of the ankle of the stance leg. In the passive dynamical model of a walking human, the upper body can be considered as an inverted pendulum jointed at the hip. Therefore, a kinematic coupling has been used in the model to keep the upper body between the two legs and achieve stable walking (Wisse *et al.*, 2004). The equation of the kinematic coupling constraint is introduced according to Eq. 20.  $2\theta_3 - (\theta_1 + \theta_2) = 0$  (20)

The time course of hip, knee, and ankle joint angles for the proposed model are given in Eqs. 21-23 (Karimi *et al.*, 2020).

$$\theta_2 - \theta_3 = 373.64t^3 - 762.66t^2 + 414.86t - 38.89 \quad (21)$$

$$\theta_{2s} - \theta_2 = -6357.5t^3 + 4911.3t^2 - 958.48t + 1.24 \quad (22)$$

$$\theta_1 = 451.84t^3 - 513.31t^2 + 218.5t - 27.77 \tag{23}$$

According to Eq. 4, the constraint equations (Eqs. 18-23) can be considered in differential form, as defined in Eqs. 24-29:

$$\dot{y}_h + l\sin\theta_1\theta_1 = 0 \tag{24}$$

$$\dot{x}_h + l\cos\theta_{\rm i}\dot{\theta}_{\rm i} = 0 \tag{25}$$

$$\dot{\theta}_1 + \dot{\theta}_2 - 2\dot{\theta}_3 = 0$$
 (26)

$$\theta_2 - \theta_3 - 1120.92t^2 + 1525.32t - 414.86 = 0 \tag{27}$$

$$\theta_2 - \theta_{2s} - 19072.5t^2 + 9822.6t - 958.48 = 0$$
 (28)

$$\dot{\theta}_1 - 1355.52t^2 + 1026.62t - 218.5 = 0$$
 (29)

By applying Lagrange's equation (Eq. 3) and introducing the constant coefficients, seven coupled non-linear differential equations of motion can be obtained (Eqs. 30-36).

 $\begin{aligned} &\eta_{i}\ddot{x}_{h} + \eta_{2}\cos\theta_{1}\ddot{\theta}_{-} - \eta_{3}\cos\theta_{2}\ddot{\theta}_{2} + \left[\eta_{4}\cos\theta_{3} + \eta_{5}\sin\theta_{3}\right]\ddot{\theta}_{3} - \eta_{6}\cos\theta_{2,s} \\ &-\eta_{7}\sin\theta_{2,f}\ddot{\theta}_{2,f} - \eta_{2}\sin\theta_{1}\dot{\theta}_{1}^{2} + \eta_{3}\sin\theta_{2}\dot{\theta}_{2}^{2} - \left[\eta_{4}\sin\theta_{3} - \eta_{5}\cos\theta_{3}\right]\dot{\theta}_{3}^{2} \\ &+\eta_{6}\sin\theta_{2,s}\dot{\theta}_{2,s}^{2} - \eta_{7}\cos\theta_{2,f}\dot{\theta}_{2,f}^{2} + \lambda_{2} = m_{0}e\omega^{2}\cos(\omega t) \\ &\eta_{i}\ddot{y}_{h} + \eta_{2}\sin\theta_{i}\dot{\theta}_{i} + \eta_{3}\sin\theta_{2}\dot{\theta}_{2} - \left[\eta_{4}\sin\theta_{3} - \eta_{5}\cos\theta_{3}\right]\ddot{\theta}_{3} + \eta_{6}\sin\theta_{2,s}\ddot{\theta}_{2,s} \\ &-\eta_{7}\cos\theta_{2,f}\ddot{\theta}_{2,f} + \eta_{2}\cos\theta_{1}\dot{\theta}_{1}^{2} + \eta_{3}\cos\theta_{2}\dot{\theta}_{2}^{2} - \left[\eta_{4}\cos\theta_{3} + \eta_{5}\sin\theta_{3}\right]\dot{\theta}_{3}^{2} \\ &+\eta_{6}\cos\theta_{2,}\dot{\theta}_{2,s}^{2} + \eta_{7}\sin\theta_{2,}\dot{\theta}_{2,s}^{2} + \lambda_{s} = m_{0}e\omega^{2}\sin(\omega t) \end{aligned}$ 

$$\begin{aligned} &\eta_{10}\ddot{\theta}_{2} - \eta_{3}\cos\theta_{1}\ddot{x}_{k} + \eta_{3}\sin\theta_{2}\ddot{y}_{k} + \eta_{11}\cos(\theta_{2} - \theta_{2})\dot{\theta}_{2s}^{2} + \eta_{12}\sin(\theta_{2f} - \theta_{2})\dot{\theta}_{2f}^{2} \\ &+ \eta_{11}\sin(\theta_{2} - \theta_{2s})\dot{\theta}_{2s}^{2} + \eta_{12}\cos(\theta_{2f} - \theta_{2})\dot{\theta}_{2f}^{2} + \eta_{3g}\sin\theta_{2} + \lambda_{3} + \lambda_{4} + \lambda_{5} \\ &= 0.0007(\theta_{2} - \theta_{3})^{3} - 0.0258(\theta_{2} - \theta_{3})^{2} + 0.3236(\theta_{2} - \theta_{3}) - 1.6792 \\ &\eta_{13}\ddot{\theta}_{3} + (\eta_{4}\cos\theta_{3} + \eta_{5}\sin\theta_{3})\ddot{x}_{h} - (\eta_{4}\sin\theta_{3} - \eta_{5}\cos\theta_{3})\ddot{y}_{h} - \eta_{4}g\sin\theta_{3} \\ &+ \eta_{5g}\cos\theta_{3} - 2\lambda_{3} - \lambda_{4} = m_{0}e\omega^{2}\cos\omega t[(c_{h} + y_{sp})\cos\theta_{3} + x_{sp}\sin\theta_{3}] \\ &- m_{0}e\omega^{2}\sin\omega t[(c_{h} + y_{sp})\sin\theta_{3} - x_{sp}\cos\theta_{3}] \\ &\eta_{i4}\ddot{\theta}_{2s} - \eta_{6}\cos\theta_{2s}\ddot{x}_{h} + \eta_{6}\sin\theta_{2s}\ddot{y}_{h} + \eta_{11}\cos(\theta_{2} - \theta_{2s})\ddot{\theta}_{2} + \eta_{15}\sin(\theta_{2f} - \theta_{2s})\ddot{\theta}_{2f} \\ &- \eta_{11}\sin(\theta_{2} - \theta_{2s})\dot{\theta}_{2}^{2} + \eta_{5}\dot{\theta}_{2}^{2}\cos(\theta_{2f} - \theta_{2s}) + \eta_{6}g\sin\theta_{2s} - \lambda_{5} = \\ &= -0.0011(\theta_{2s} - \theta_{2})^{2} - 0.0029(\theta_{2s} - \theta_{2}) + 1.2683 \\ c_{f}\ddot{\theta}_{2f} - \sin\theta_{2f}\ddot{x}_{h} - \cos\theta_{2f}\ddot{y}_{h} + l_{r}\sin(\theta_{2f} - \theta_{2})\ddot{\theta}_{2}^{2} + l_{s}\sin(\theta_{2f} - \theta_{2s})\ddot{\theta}_{2s} \\ &- l_{r}\cos(\theta_{2f} - \theta_{2})\dot{\theta}_{2}^{2} - l_{r}\cos(\theta_{2f} - \theta_{2s})\dot{\theta}_{2s}^{2} - g\cos\theta_{2f} = 0 \end{aligned} \tag{36}$$

The constant coefficients  $\eta_i$  (i=1, 2, ..., 15) are defined in the Appendix. Thirteen coupled non-linear differential equations (Eqs. 24-36) for  $x_h$ ,  $y_h$ ,  $\theta_1$ ,  $\theta_2$ ,  $\theta_3$ ,  $\theta_{2s}$ ,  $\theta_{2f}$ ,  $\lambda_1$ ,  $\lambda_2$ ,  $\lambda_3$ ,  $\lambda_4$ ,  $\lambda_5$ , and  $\lambda_6$  must be solved to analyze the dynamical behavior of the operator's body during working with a motorized backpack sprayer.

# Hip and ankle joint forces in the swing phase

Forces in the human joints are important factors in the initiation and progression stages of joint diseases. Investigation of the joint forces has made it possible to prevent or minimize discomfort, fatigue, or risk of injuries. In this section, the hip and ankle joint forces in the model of the operator's body while working with a motorized backpack sprayer are calculated. Considering the upper body, Newton's second law leads to Eqs. 37 and 38.

$$\sum F_x = m_b \ddot{x}_{m_b} + m_{sp} \ddot{x}_{m_{sp}} + m_0 e \omega^2 \cos(\omega t)$$
(37)

$$\sum F_{y} = m_{b} \ddot{y}_{m_{b}} + m_{sp} \ddot{y}_{m_{sp}} + m_{0} e \omega^{2} \sin(\omega t)$$
(38)

The components of the hip joint force then become Eqs. 39 and 40.

$$F_{x_{b}} = m_{b}(\ddot{x}_{b} + c_{b}\cos\theta_{3}\ddot{\theta}_{3}) + m_{sp}(\ddot{x}_{b} + x_{sp}\sin\theta_{3}\ddot{\theta}_{3} + (c_{b} + y_{sp})\cos\theta_{3}\ddot{\theta}_{3}) + m_{p}e\omega^{2}\cos(\omega t)$$
(39)

$$F_{y_{h}} = m_{b}(\ddot{y}_{h} - c_{b}\sin\theta_{3}\ddot{\theta}_{3}) + m_{sp}(\ddot{y}_{h} + x_{sp}\cos\theta_{3}\ddot{\theta}_{3} - (c_{b} + y_{sp})\sin\theta_{3}\ddot{\theta}_{3}) + m_{b}e\omega^{2}\sin(\omega t) + (m_{sp} + m_{b})g$$
(40)

Finally, the total hip joint force can be calculated using Eq. 41.

$$F_{h} = \sqrt{F_{x_{h}}^{2} + F_{y_{h}}^{2}}$$
(41)

Considering the full body, Newton's second law leads to Eq. 42.

 $\sum F_{x} = m_{b} \ddot{x}_{m_{b}} + m_{f} \ddot{x}_{m_{f}} + m_{h} \ddot{x}_{m_{s}} + m_{f} \ddot{x}_{m_{t}} + m_{s} \ddot{x}_{m_{s}} + m_{sp} \ddot{x}_{m_{sp}} + m_{t} \ddot{x}_{m_{t}} + m_{0} c \omega^{2} \cos(\omega t)$ (42)

And the x-directional force of the hip joint is expressed in Eq. 43.

$$F_{x_{f}} = m_{b}(\ddot{x}_{h} + c_{b}\cos\theta_{3}\ddot{\theta}_{3}) + m_{f}(\ddot{x}_{h} - l_{s}\cos\theta_{2}, \ddot{\theta}_{2s} - l_{r}\cos\theta_{2}\ddot{\theta}_{2} - c_{f}\sin\theta_{2f}\ddot{\theta}_{2f}) + m_{h}\ddot{x}_{h} + m_{l}(l - c_{l})\cos\theta_{l}\ddot{\theta}_{l} + m_{s}(\ddot{x}_{h} - c_{s}\cos\theta_{2s}\ddot{\theta}_{2s} - l_{r}\cos\theta_{2}\ddot{\theta}_{2}) + m_{sp}(\ddot{x}_{h} + x_{sp}\sin\theta_{3}\ddot{\theta}_{3} + (c_{b} + y_{sp})\cos\theta_{3}\ddot{\theta}_{3}) + m_{r}(\ddot{x}_{h} - c_{r}\cos\theta_{2}\ddot{\theta}_{2}) + m_{0}e\omega^{2}\cos(\omega t)$$

$$(43)$$

Considering the leg stance, the calculation of the moment about the hip joint leads to Eq. 44.

$$F_{y_f} = m_l c_l (l - c_l) \theta_1 + m_l g c_l \sin \theta_1 - F_{x_f} l \cos \theta_1 / l \sin \theta_1 \qquad (44)$$

Finally, the total ankle joint force is calculated using Eq. 45.

$$F_{f} = \sqrt{F_{x_{f}}^{2} + F_{y_{f}}^{2}}$$
(45)

# **Results and Discussion**

The values of the physical parameters related to this analysis are listed in Table 1. Thirteen coupled non-linear differential equations (Eqs. 24-36) are solved in Maple software. Fig. 2 illustrates the effects of engine speed and mass of the sprayer on the hip and ankle joint forces during working with a motorized backpack sprayer.

It can be observed that the ankle force fluctuates at the beginning of the swing phase (t=[0.1-0.2]). It remains relatively constant in the middle of the swing phase t=[0.2-0.4] and again fluctuates at the end of the swing phase (t=[0.4-0.5]). The first fluctuation occurs because of the 'toe-off'. In the 'toe-off' instance, the toe loses contact with the ground. The second fluctuation was caused by the 'heel-strike'. In this instance, there is an impact between the leg swing and the ground when the heel of the swinging leg comes into contact with the ground. The maximum force is exerted on the joints when the operator begins to swing forward ('toe-off'). Furthermore, in the instances of 'toe-off' and 'heel-strike', undesirable variations of ankle joint force  $F_h$  are noticeable. This means that ankle injuries due to vibration exposure are more likely.

**Table 1-** The values of physical parameters (Huang *et al.*, 2012)

Parameter	Value
Distance from hip joint to CoM of the upper body, cb	0.262 m
Distance from the ankle joint to CoM of the foot, cf	0.017 m
Distance from the knee joint to CoM of shank, cs	0.157 m
Distance from hip joint to CoM of the thigh, ct	0.192
Unbalance mass eccentricity, e	5 mm
Gravitational acceleration, g	$9.81 \text{ m s}^{-2}$
Mass moments of inertia of sprayer about its principal axis, $I_{sp}$	kg.m <sup>2</sup>
Stance leg length, <i>l</i>	0.700 m
Shank length, <i>l</i> <sub>s</sub>	0.315 m
Thigh length, $l_t$	0.385 m
Unbalance mass of sprayer engine, $m_o$	0.01 gr
Upper body mass, $m_b$	26.62 kg
Foot mass, $m_f$	2.66 kg
Hip mass, $m_h$	19.97 kg
Leg mass, $m_l$	11.53 kg
Shank mass, <i>m</i> <sub>s</sub>	3.45 kg
Sprayer mass, $m_{sp}$	10.50 kg
Thigh mass, $m_t$	8.07 kg
Sprayer position from the CoM of upper body, $(x_{sp}, y_{sp})$	(0.175m, 0.038m)
Engine speed, $\omega$	3000 rpm

From a comparison between Fig. 2 (a) and (b) it is revealed that the frequency of the hip joint force increases with increased engine speed ( $\omega$ ). However, considerable effects on the frequency of the ankle joint force have not been observed. Additionally, with increasing the engine speed ( $\omega$ ), amplitudes of both the hip and ankle joint forces increase.

From a comparison between Fig. 2 (a) and (c) it can be concluded that increasing the mass of the sprayer (msp) leads to a small reduction in the oscillation of the ankle joint force. Moreover, as the mass of the sprayer

(msp) increases, the magnitude of both the hip and ankle joint forces increases as well.

Fig. 3 exhibits the effect of leg length on the hip and ankle joint forces while working with a motorized backpack sprayer. It can be observed that the frequency of the hip joint force increases with decreasing the leg length l. This is because the leg stance keeps contact with the ground while the leg swings and pivots about the constrained hip like a pendulum. So, shorter operators are more vulnerable to injuries due to vibration exposure.













Fig.3. The hip joint force  $F_h$  and ankle joint force  $F_f$  for  $m_{sp}$ =10.5 kg,  $\omega$ =3000 rpm, and (a) l=0.7 m, (b) l=0.7 m, and (c) l=0.7 m

# Conclusion

In this study, a novel assistive dynamical model for the operator's body while working with a motorized backpack sprayer was presented. In this model, the coordinate of the sprayer relative to the body, rotational inertia of the sprayer, muscle moments acting on joints, and a kinematic coupling confining the upper body between the two legs were considered. The dynamics of the sprayer's described operator were using seven coordinates. The non-linear generalized equations of motion were obtained using the Lagrangian equations. The results obtained from the numerical analysis indicated that, at the beginning and end of the swing phase, ankle injuries due to vibration exposure are more probable. Moreover, the maximum force is exerted on the joints at the beginning of the swing phase. Furthermore, the effects of engine speed and mass of the sprayer on the hip and ankle joint forces were studied. It was found that the larger mass of the sprayer (full capacity of the tank) can lead to higher levels of joint forces and lower oscillations. The frequency of hip and ankle joint forces increased with the increase of the engine speed. The results of this paper can be used for an estimated evaluation of a patient's condition and implant design. Investigation of the effects of anthropometric specifications

and sprayer position (relative to the body) on the hip and ankle joint forces while working with a motorized backpack sprayer are valuable topics for further studies.

# **Key Points**

- Development of a seven-link dynamic model of the operator's body while working with a motorized backpack sprayer
- The non-linear differential equations of motion are formulated using Lagrangian equations and solved in Maple software
- Study of the effects of engine speed and mass of sprayer on the hip and ankle joint forces

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# Appendix

The constant coefficients for Eqs. 30-36 are as follows:

$$\begin{split} \eta_{1} &= m_{h} + m_{l} + m_{t} + m_{b} + m_{sp} + m_{s} + m_{f} & \eta_{2} = m_{l}c_{l} \\ \eta_{3} &= m_{t}c_{t} + m_{s}l_{t} + m_{f}l_{t} & \eta_{4} = m_{b}c_{b} + m_{sp}\left(c_{b} + y_{sp}\right) \\ \eta_{5} &= m_{sp}x_{sp} & \eta_{6} = m_{s}c_{s} + m_{f}l_{s} \\ \eta_{7} &= m_{f}c_{f} & \eta_{8} = m_{l}c_{l}^{2} \\ \eta_{9} &= \eta_{1}l - m_{l}c_{l} & \eta_{10} = m_{t}c_{l}^{2} + m_{s}l_{t}^{2} + m_{f}l_{t}^{2} \\ \eta_{11} &= l_{t}\eta_{6} & \eta_{12} = m_{f}l_{t}c_{f} \\ \eta_{13} &= I_{sp} + m_{b}c_{b}^{2} + m_{sp}\left[\left(c_{b} + y_{sp}\right)^{2} + x_{sp}^{2}\right] & \eta_{14} = m_{s}c_{s}^{2} + m_{f}l_{s}^{2} \\ \eta_{15} &= m_{f}l_{s}c_{f} \end{split}$$

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مقاله پژوهشی

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مدلسازی دینامیکی بار وارد بر مفاصل ران و مچ پا، هنگام کار با سمپاش پشتی موتوری

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# چکیدہ

هدف اصلی این مقاله توسعه یک مدل دینامیک هفت لینکی از بدن اپراتور در هنگام کار با سمپاش کولهپشتی موتوری است. این مدل شامل مختصات سمپاش نسبت به بدن، اینرسی چرخشی سمپاش، گشتاور ماهیچهای وارد بر روی مفاصل و یک کوپلینگ سینماتیکی است که تعادل بـدن را بین دو پا حفظ می کند. توابع قید تعیین شدند و معادلات دیفرانسیل غیرخطی حرکت توسط معادلات لاگرانژ استخراج گردیدند. نتایج نشان میدهد کـه در ابتدا و انتهای مرحله شناوری، تغییرات نامطلوب نیروی مفصل مچ پا قابل توجه است. بنابراین، آسیب مچ پا به دلیل قرار گرفتن در معرض ارتعاش احتمال بیشتری دارد. سپس اثرات دور موتور و جرم سمپاش بر نیروهای مفصل ران و مچ پا بررسی شد. نتایج نشان داد که دور موتور و جـرم سـمپاش اثرات قابل توجهی بر نیروهای مفصل ران و مچ پا دارد و میتواند به عنوان پارامترهای کنترلی موثر مورد استفاده قرار گرفتن در معـرض ارتعاش میدهد که با افزایش دور موتور، فرکانس نیروی مفصل ران افزایش مییابد. با این حال، اثرات قابل توجهی بر فرکانس نیروی مفصل مح پا مشاهد میدهد که با افزایش دور موتور، فرکانس نیروی مفصل ران افزایش مییابد. با این حال، اثرات قابل توجهی بر فرکانس نیروی مفصل مح پا مشاهد میدهد که با افزایش دور موتور، فرکانس نیروی مفصل ران افزایش مییابد. با این حال، اثرات قابل توجهی بر فرکانس نیروی مفصل مح پا مشاهده بروتز و محاسبات نیرویی ایمپلنتهای ران در آینده ارائه دهد.

**واژدهای کلیدی:** اپراتور، ارتعاش، معادله لاگرانژ، وزن سمپاش

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